

TADAM: Learning Timed Automata from Noisy Observations

Lénaïg Cornanguer, Pierre-François Gimenez
(equal contribution)



Introduction



system

communication protocol



industrial process

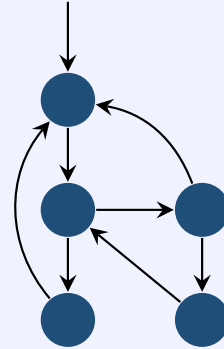
Introduction

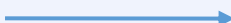


communication protocol

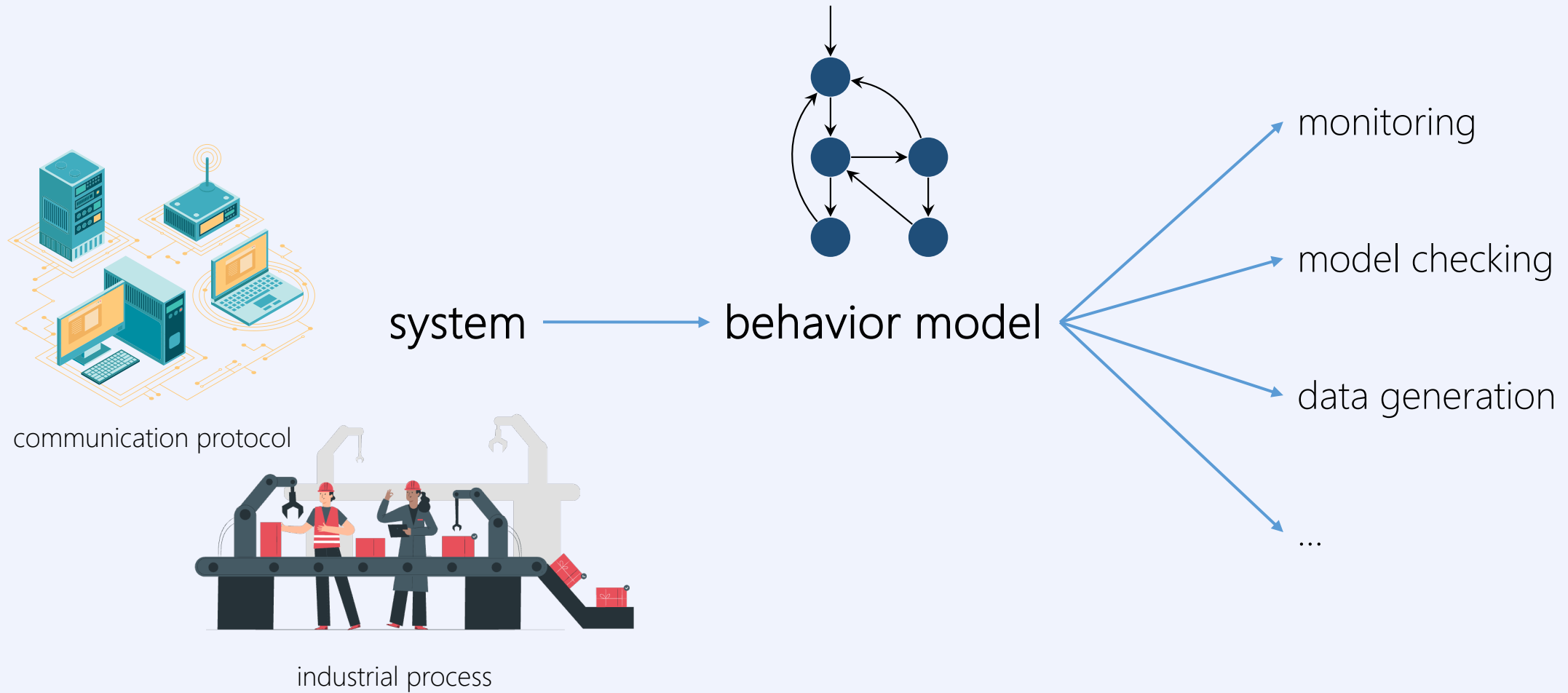


industrial process



system  behavior model

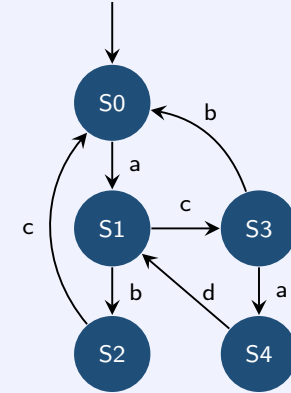
Introduction



Behavior model formalism

Automata formalism

Finite state automata (FSA)



Natural formalism for **discrete event system (DES)** modeling

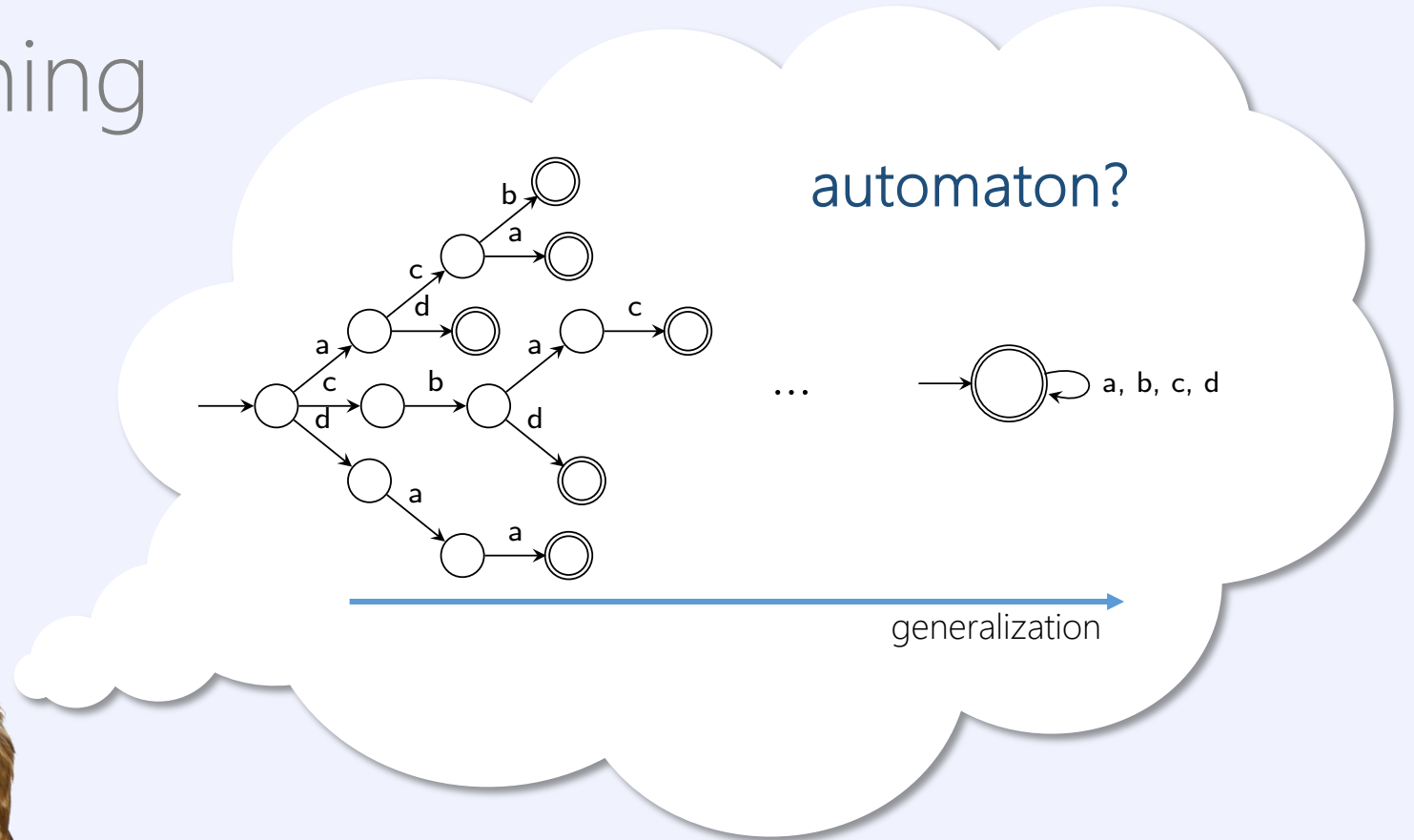
Human-understandable representation of the behavior of a system

Based on a **mathematical formalism** with **extensive literature** and with **software support**

Automata learning

data

acb
ad
cbac
aca
daa
cbd



Automata learning

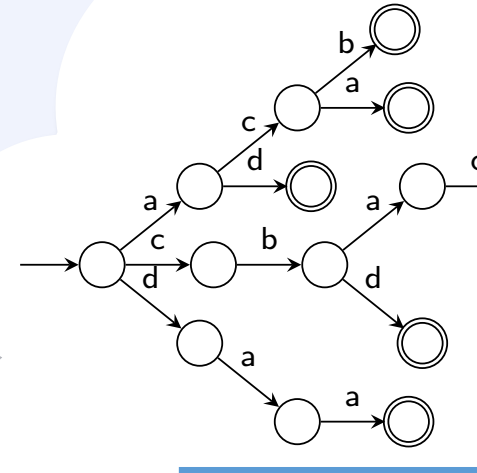


limited measurement accuracy,
probe configuration error

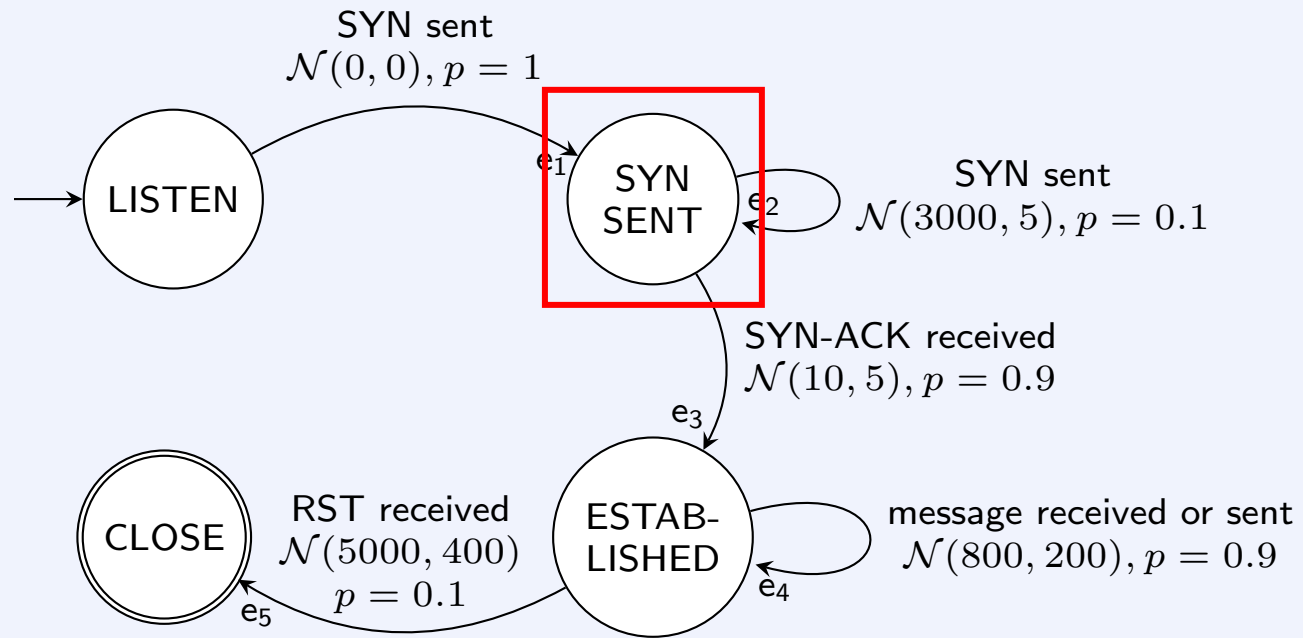
...

noisy
data

a c b
a d
c b a c
a c a
d a a
c b d

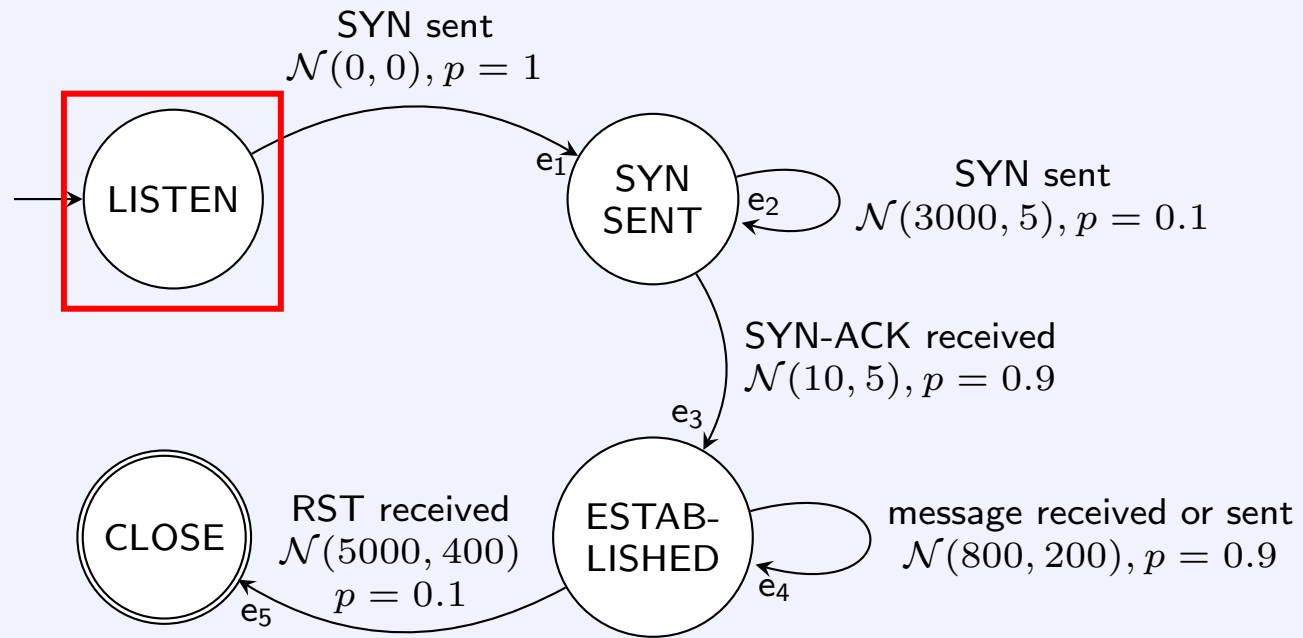


Probabilistic Real-Time Automaton



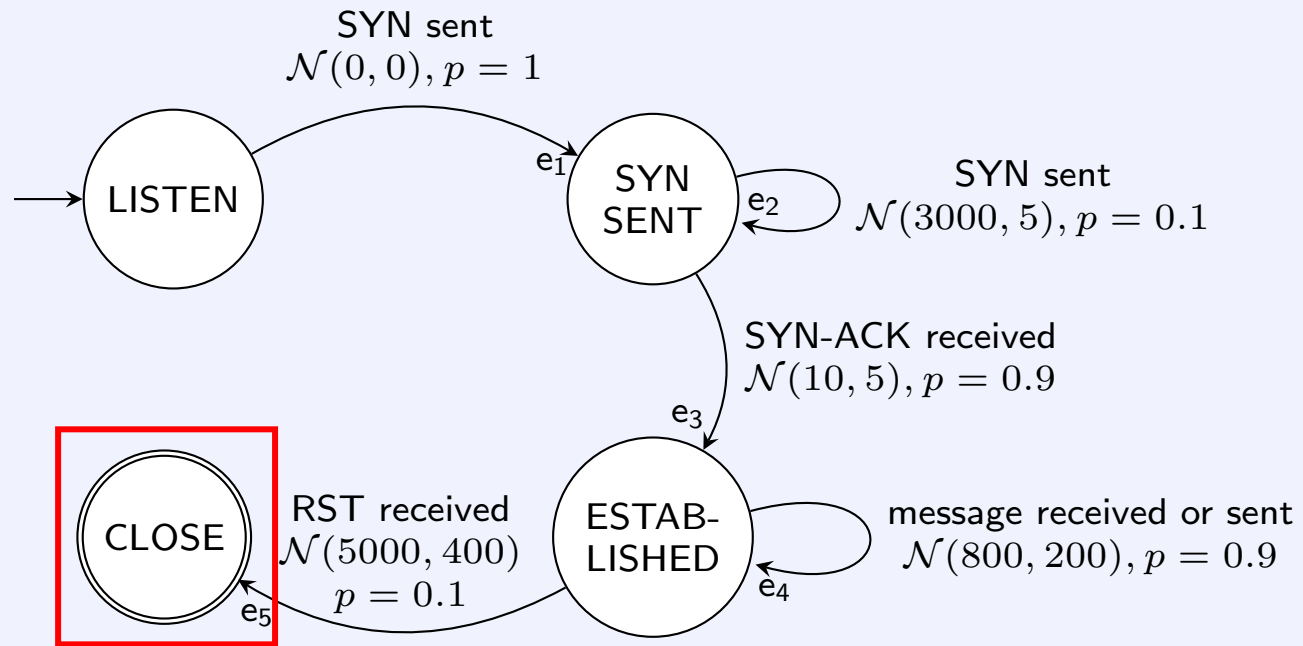
location
 $q \in \mathcal{Q}$

Probabilistic Real-Time Automaton



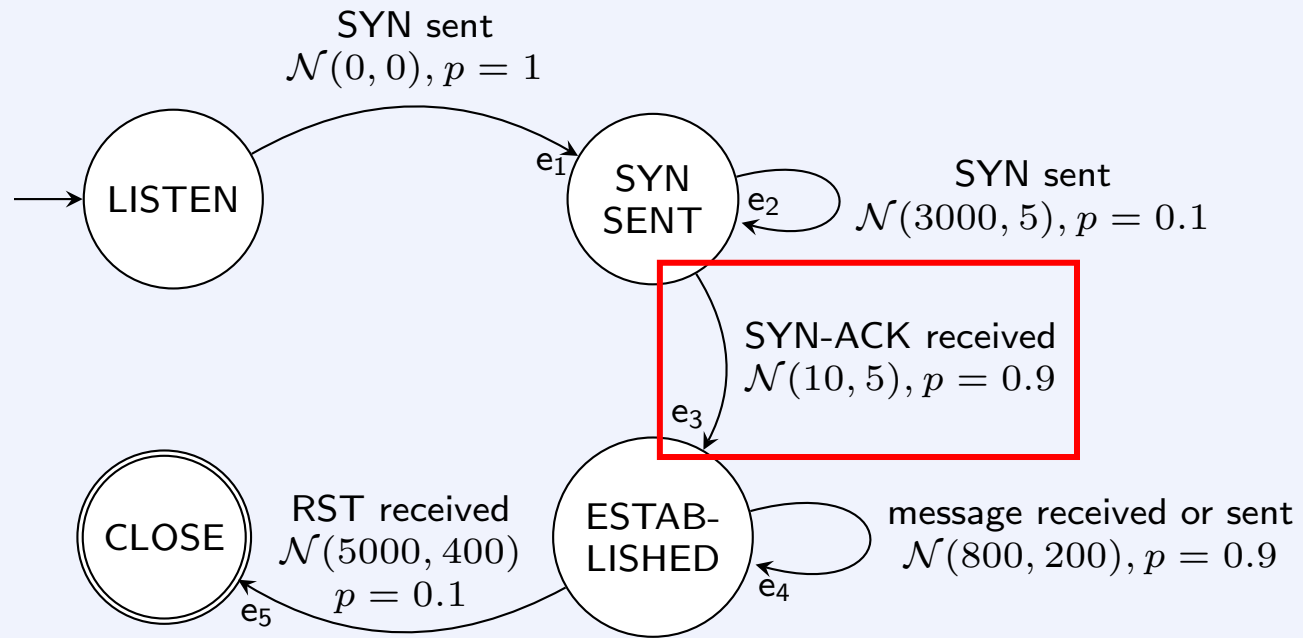
initial
location

Probabilistic Real-Time Automaton



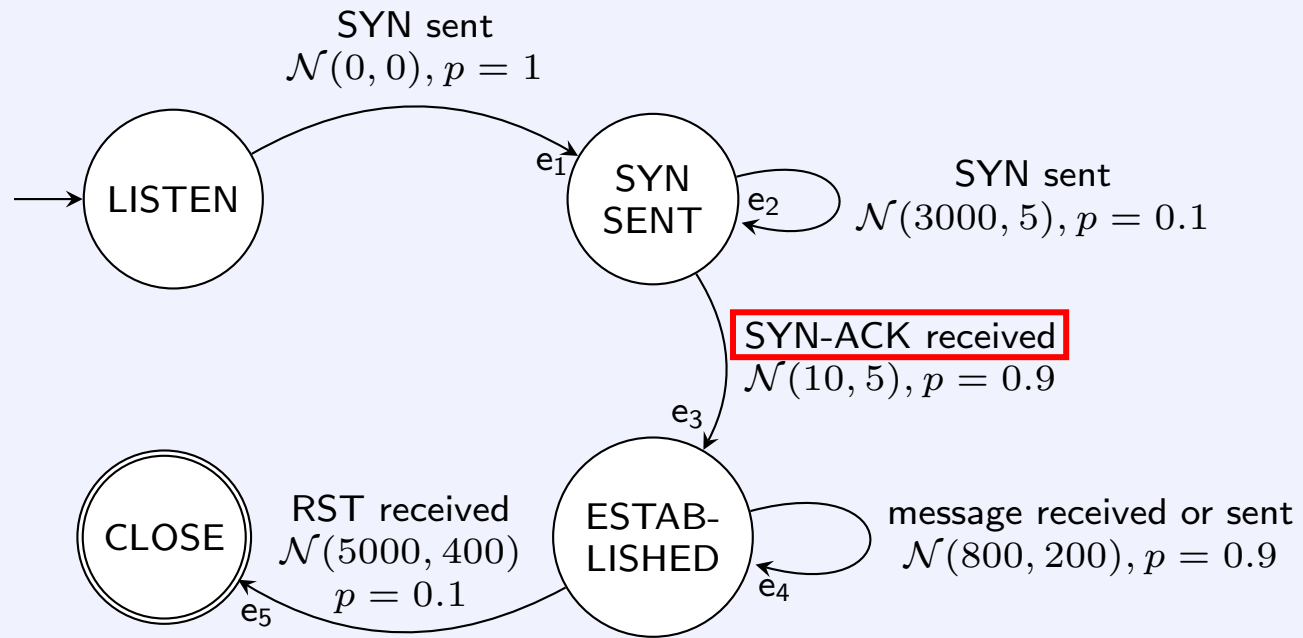
final
location

Probabilistic Real-Time Automaton



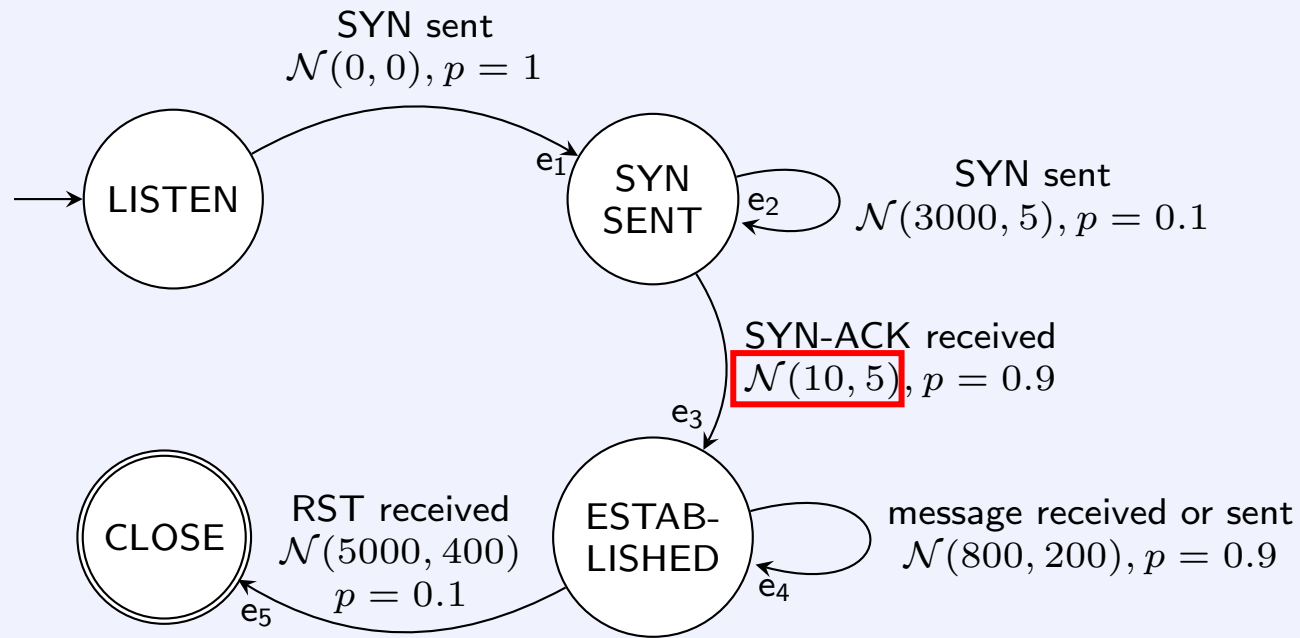
transition
 $e \in \mathcal{E}$

Probabilistic Real-Time Automaton



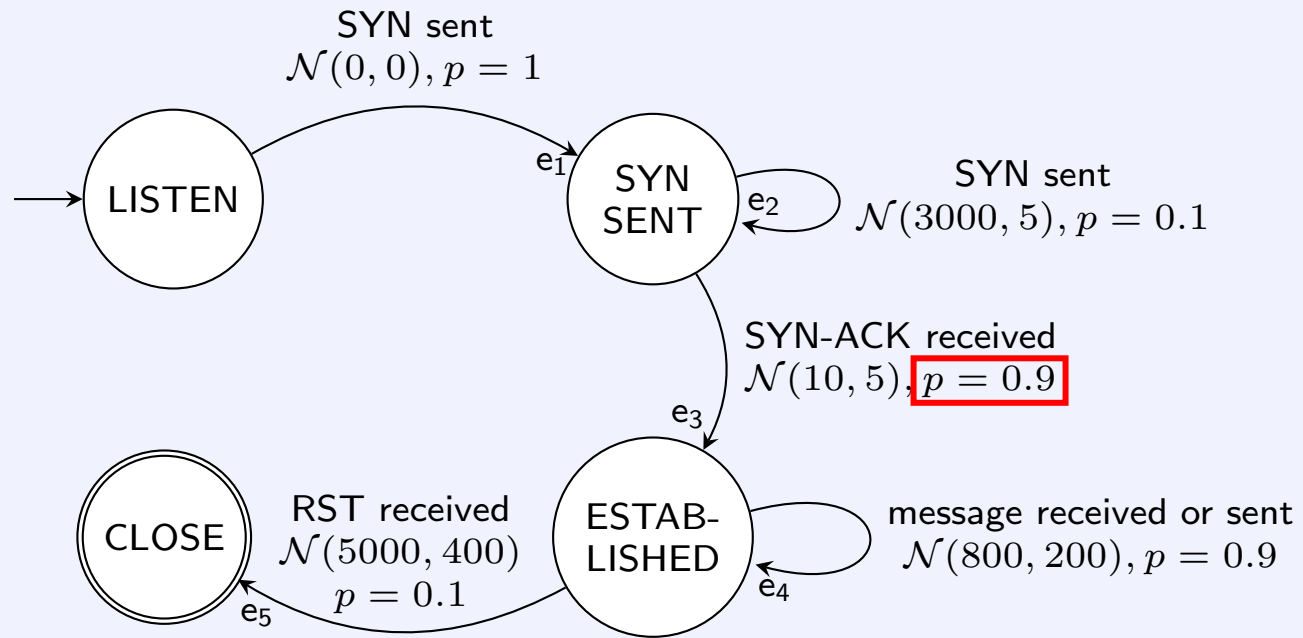
symbol
 $a \in \Sigma$

Probabilistic Real-Time Automaton



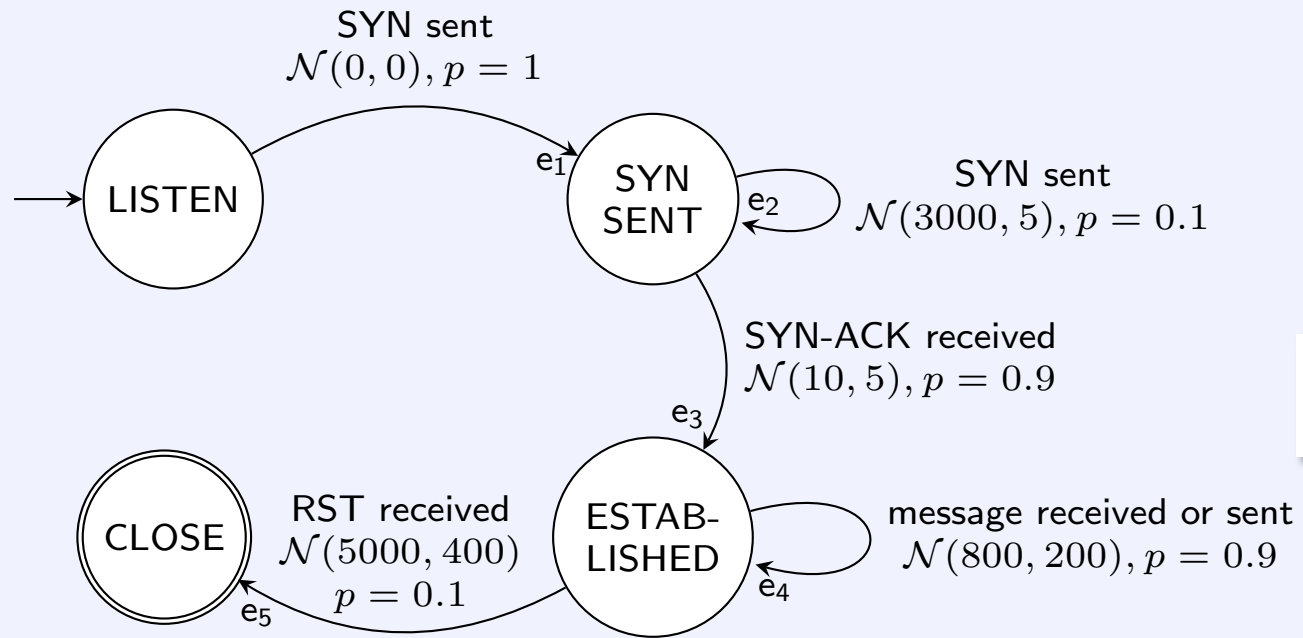
delay
distribution
 $\mathcal{N}(\mu, \sigma)$

Probabilistic Real-Time Automaton



transition
probability
 p

Probabilistic Real-Time Automaton



timed word

$(\text{SYN sent}, 0), (\text{SYN sent}, 2000), (\text{SYN-ACK received}, 10), (\text{RST received}, 6500)$

$$w = \{(a, d), \dots\}$$

Noise model

(SYN sent, 0),(SYN sent, 2000),(SYN-ACK received, 10),(RST received, 6500)

|
deletion
↓

(SYN sent, 0),(SYN sent, 2000),(RST received, 6500)

Noise model

(SYN sent, 0),(SYN sent, 2000),(SYN-ACK received, 10),(RST received, 6500)

|
insertion
↓

(SYN sent, 0),(SYN sent, 2000),(SYN-ACK received, 10),(SYN sent, 50),(RST received, 6500)

Noise model

(SYN sent, 0),(SYN sent, 2000),(SYN-ACK received, 10),(RST received, 6500)

|
transposition
↓

(SYN sent, 0),(SYN-ACK received, 10),(SYN sent, 2000),(RST received, 6500)

Noise model

(SYN sent, 0),(SYN sent, 2000),(SYN-ACK received, 10),(RST received, 6500)

|
symbol repetition
↓

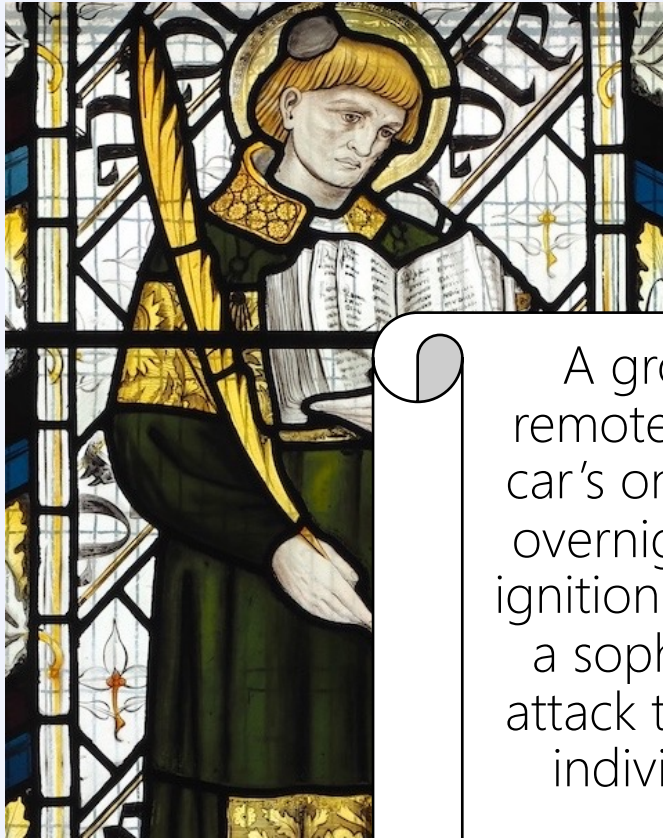
(SYN sent, 0),(SYN sent, 2000),(SYN-ACK received, 10),(SYN-ACK received, 7),(RST received, 6500)

Question



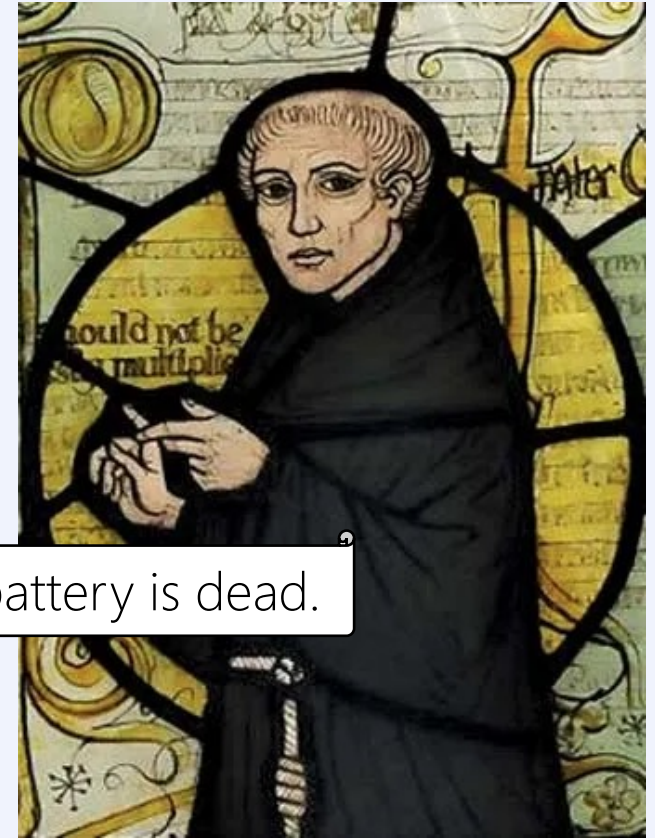
How to learn **timed automata** from **noisy** timed words?

Occam's razor



Why won't my car start?

A group of hackers remotely accessed your car's onboard computer overnight, disabling the ignition system as part of a sophisticated cyber-attack targeting random individuals to create chaos.



Your car battery is dead.

Occam's razor

The **simplest** model that fits the data is usually the correct one



MDL principle

Two-part description length


$$L(\mathcal{D}, \mathcal{A}) = L(\mathcal{D}|\mathcal{A}) + L(\mathcal{A})$$

MDL principle

Two-part description length

$$L(\mathcal{D}, \mathcal{A}) = L(\mathcal{D}|\mathcal{A}) + L(\mathcal{A})$$

global length
(# of bits needed)

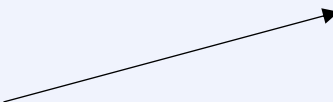


MDL principle

Two-part description length

$$L(\mathcal{D}, \mathcal{A}) = L(\mathcal{D}|\mathcal{A}) + L(\mathcal{A})$$

global length
(# of bits needed)

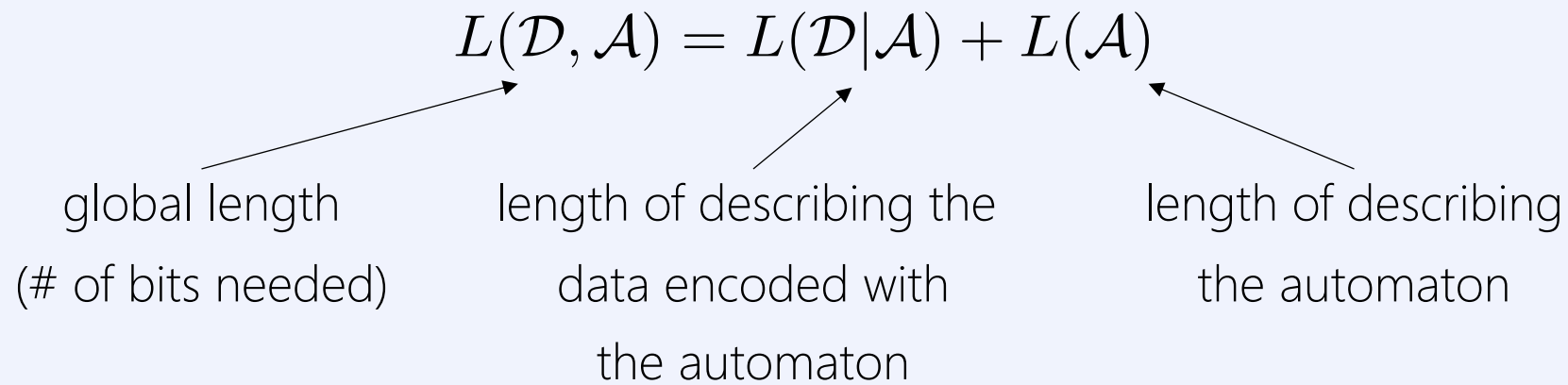


length of describing
the automaton



MDL principle

Two-part description length



MDL principle

Two-part description length

$$L(\mathcal{D}, \mathcal{A}) = L(\mathcal{D}|\mathcal{A}) + L(\mathcal{A})$$

global length
(# of bits needed)

length of describing the
data encoded with
the automaton

length of describing
the automaton

Minimum Description Length principle

$$\mathcal{A}^* = \operatorname{argmin}_{\mathcal{A} \in \mathcal{A}} L(\mathcal{D}|\mathcal{A}) + L(\mathcal{A})$$

Automaton encoding

$$L(\mathcal{A}) =$$

Automaton encoding

- Locations

$$L(\mathcal{A}) = L_{\mathbb{N}}(|Q|)$$

Automaton encoding

- Locations
- Alphabet

$$L(\mathcal{A}) = L_{\mathbb{N}}(|\mathcal{Q}|) + L_{\mathbb{N}}(|\Sigma|)$$

Automaton encoding

- Locations
- Alphabet
- Initial and accepting locations

$$L(\mathcal{A}) = L_{\mathbb{N}}(|\mathcal{Q}|) + L_{\mathbb{N}}(|\Sigma|) + 2\log_2(|\mathcal{Q}|) +$$

Automaton encoding

- Locations
- Alphabet
- Initial and accepting locations
- For each transition:

$$L(\mathcal{A}) = L_{\mathbb{N}}(|Q|) + L_{\mathbb{N}}(|\Sigma|) + 2\log_2(|Q|) +$$

$$\sum_{e \in \mathcal{E}} \left(\right)$$

Automaton encoding

- Locations
- Alphabet
- Initial and accepting locations
- For each transition:
 - Source and destination locations

$$L(\mathcal{A}) = L_{\mathbb{N}}(|\mathcal{Q}|) + L_{\mathbb{N}}(|\Sigma|) + 2\log_2(|\mathcal{Q}|) +$$

$$\sum_{e \in \mathcal{E}} \left(2\log_2(|\mathcal{Q}|) \right)$$

Automaton encoding

- Locations
- Alphabet
- Initial and accepting locations
- For each transition:
 - Source and destination locations
 - Symbol

$$L(\mathcal{A}) = L_{\mathbb{N}}(|\mathcal{Q}|) + L_{\mathbb{N}}(|\Sigma|) + 2\log_2(|\mathcal{Q}|) +$$

$$\sum_{e \in \mathcal{E}} \left(2\log_2(|\mathcal{Q}|) + \log_2(|\Sigma|) + \right)$$

Automaton encoding

- Locations
- Alphabet
- Initial and accepting locations
- For each transition:
 - Source and destination locations
 - Symbol
 - Guards' normal distributions parameters

$$L(\mathcal{A}) = L_{\mathbb{N}}(|\mathcal{Q}|) + L_{\mathbb{N}}(|\Sigma|) + 2\log_2(|\mathcal{Q}|) +$$

$$\sum_{e \in \mathcal{E}} \left(2\log_2(|\mathcal{Q}|) + \log_2(|\Sigma|) + \right. \\ \left. L_{\mathbb{N}}(\lfloor \mu_e \rfloor) + L_{\mathbb{N}}(\lfloor \sigma_e^2 \rfloor) \right)$$

Data encoding

1. **Correct** the non-accepted words to **remove the noise**
2. **Encode the corrected data**

Data correction

Noise type	Correction operation
deletion aab b cad → aacad	add
insertion aabcbad → aabcb a d	skip
transposition aabcbad → aac b ad	transpose
symbol repetition aabcbad → aabcb a ad	deduplicate
—	follow

Data correction

edit operation sequence

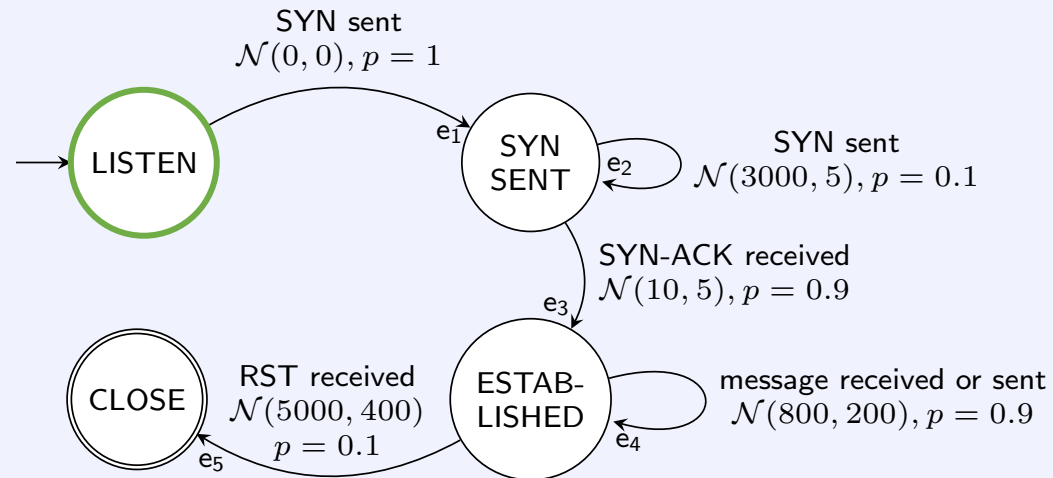
{operation, transition to use, delay}

word

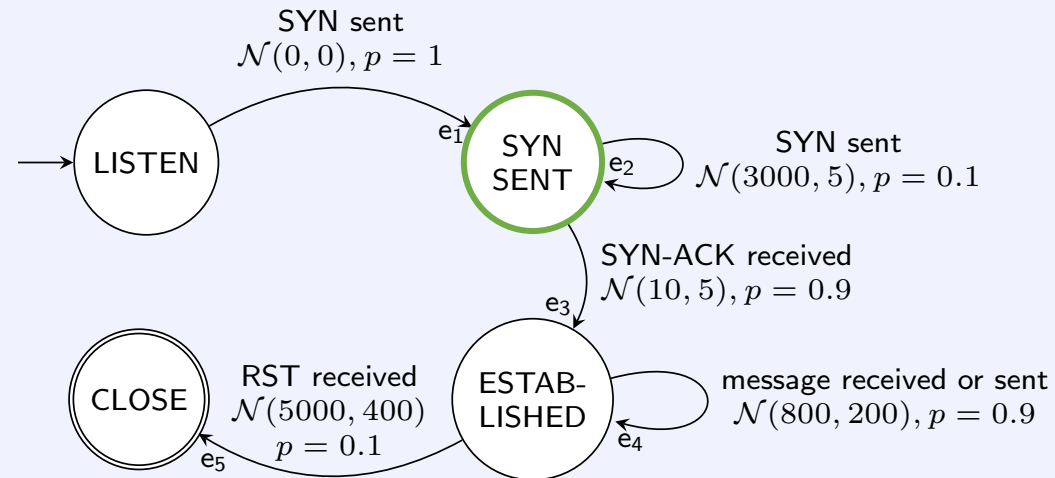
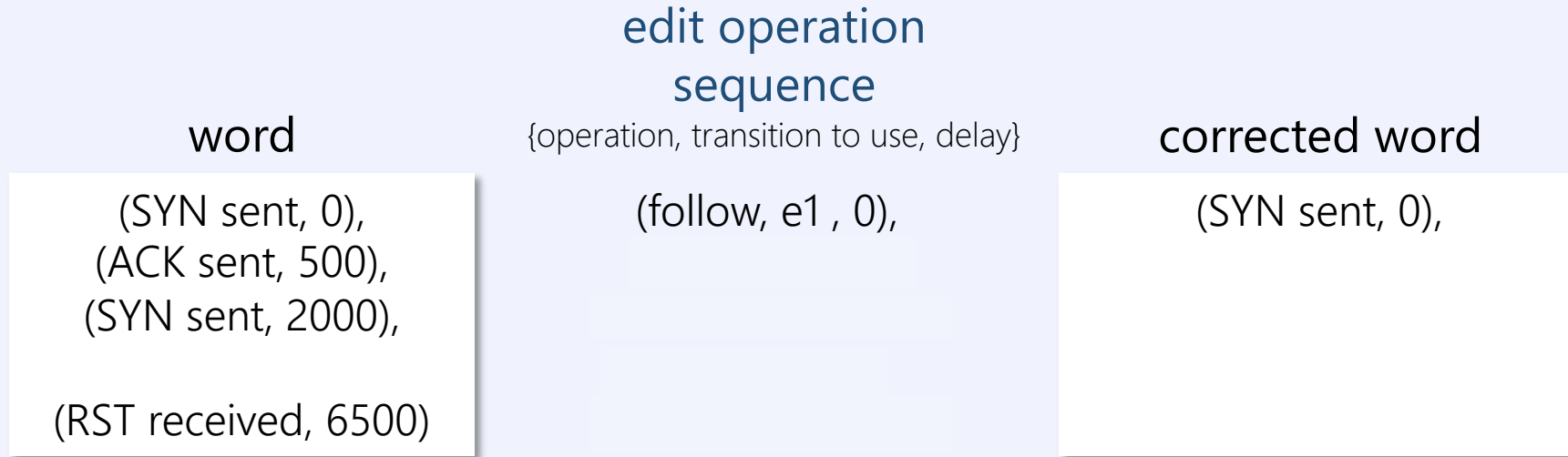
(SYN sent, 0),
(ACK sent, 500),
(SYN sent, 2000),

(RST received, 6500)

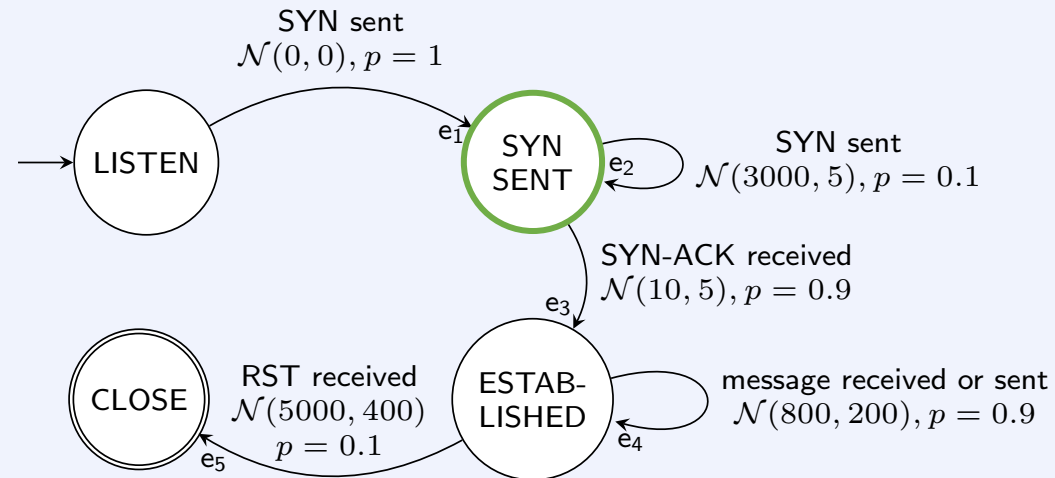
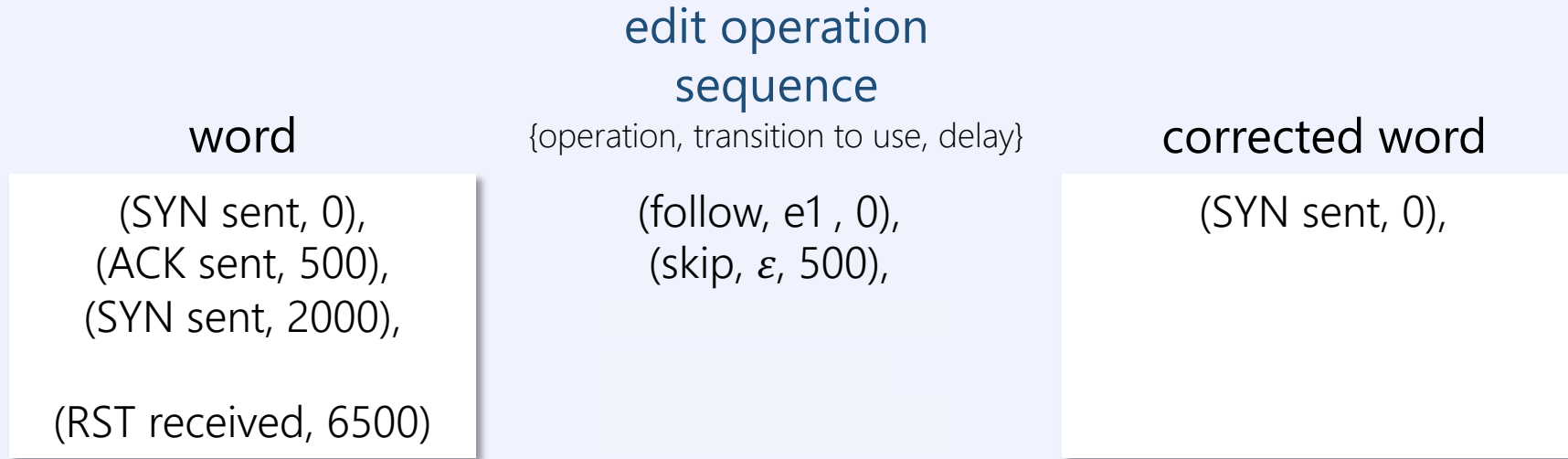
corrected word



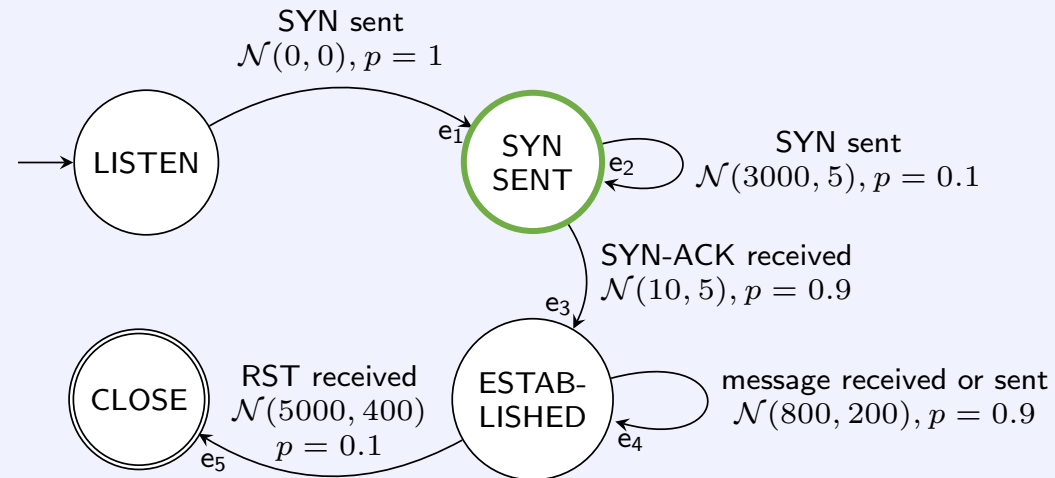
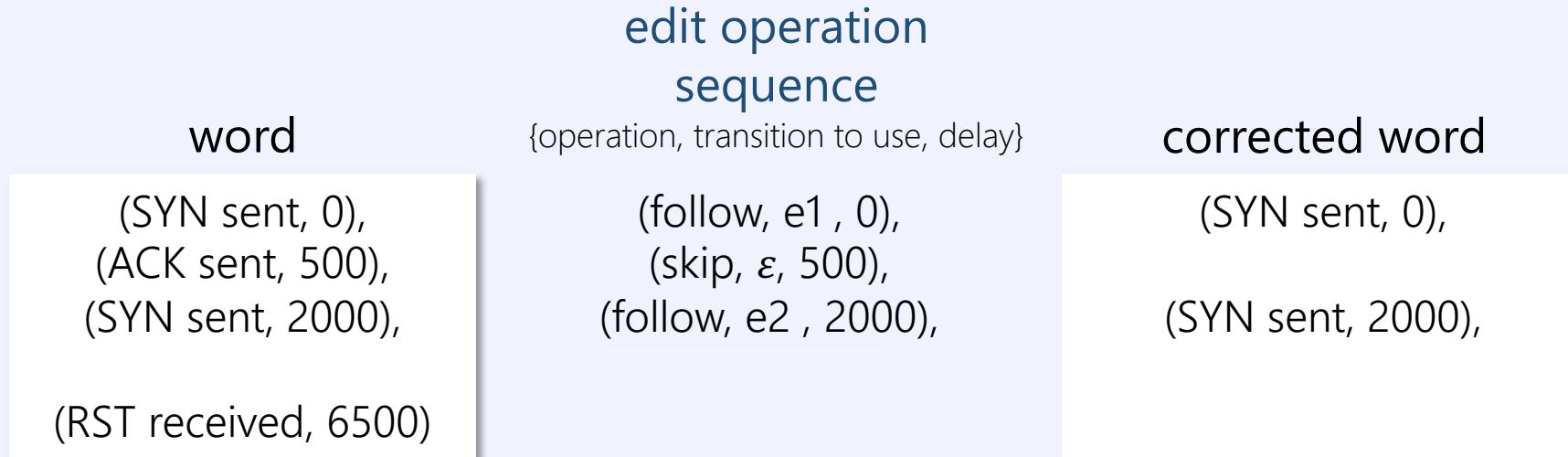
Data correction



Data correction



Data correction



Data correction

edit operation sequence

{operation, transition to use, delay}

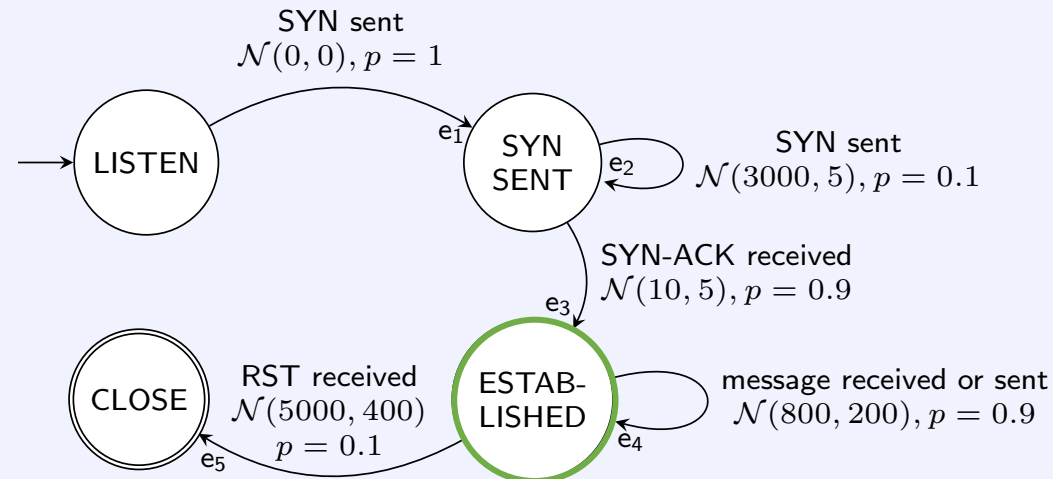
word

(SYN sent, 0),
(ACK sent, 500),
(SYN sent, 2000),
(RST received, 6500)

corrected word

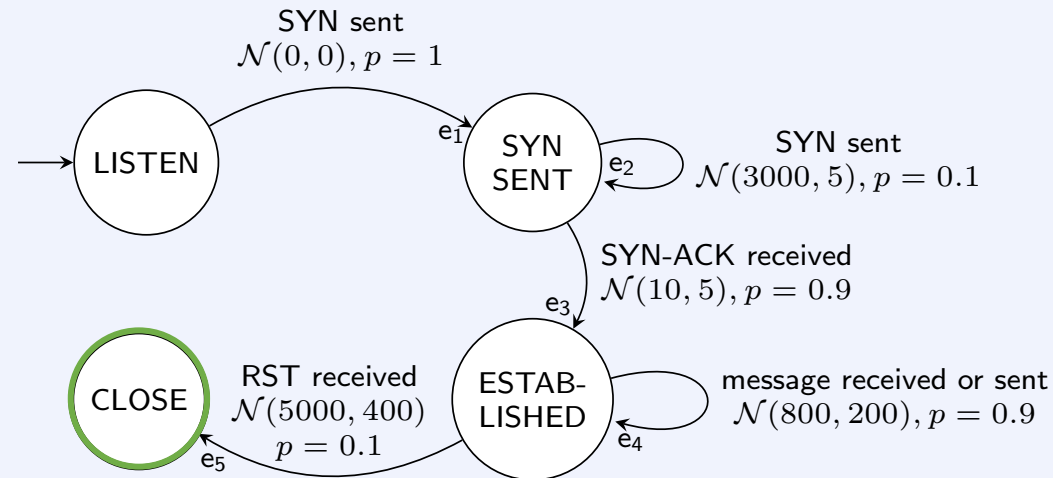
(SYN sent, 0),

(SYN sent, 2000),
(SYN-ACK received, 10),



Data correction

word	edit operation sequence <small>{operation, transition to use, delay}</small>	corrected word
(SYN sent, 0), (ACK sent, 500), (SYN sent, 2000), (RST received, 6500)	(follow, e1, 0), (skip, ε , 500), (follow, e2, 2000), (add, e3, 10), (follow, e5, 6500)	(SYN sent, 0), (SYN sent, 2000), (SYN-ACK received, 10), (RST received, 6500)



Data correction

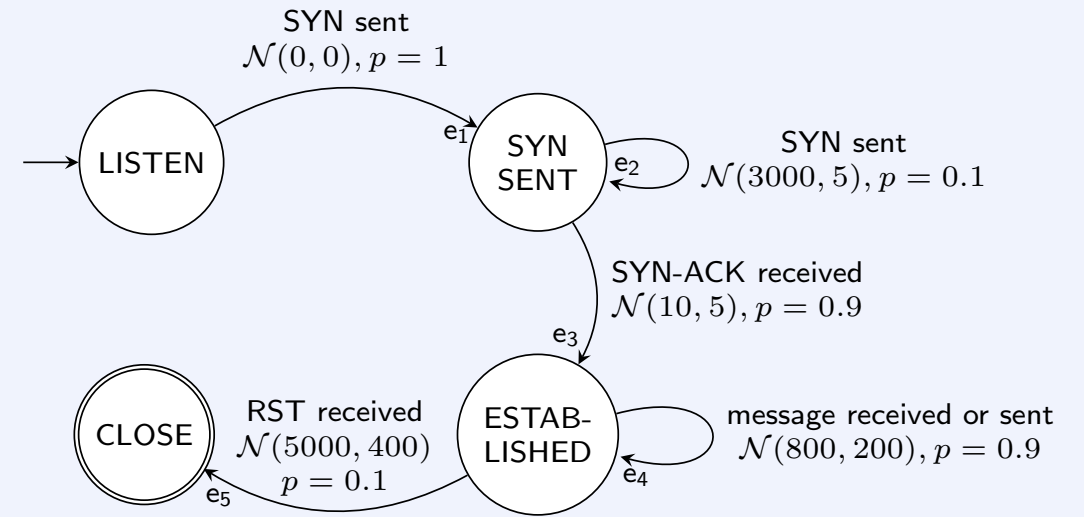
(SYN sent, 0),(ACK sent, 500),(SYN sent, 2000),(RST received, 6500)

correction

(SYN sent, 0),(SYN-ACK received, 10),(RST received, 6500)

(SYN sent, 0),(SYN sent, 2000),(SYN-ACK received, 10),(RST received, 6500)

...



Many correction solutions possible...

Data correction

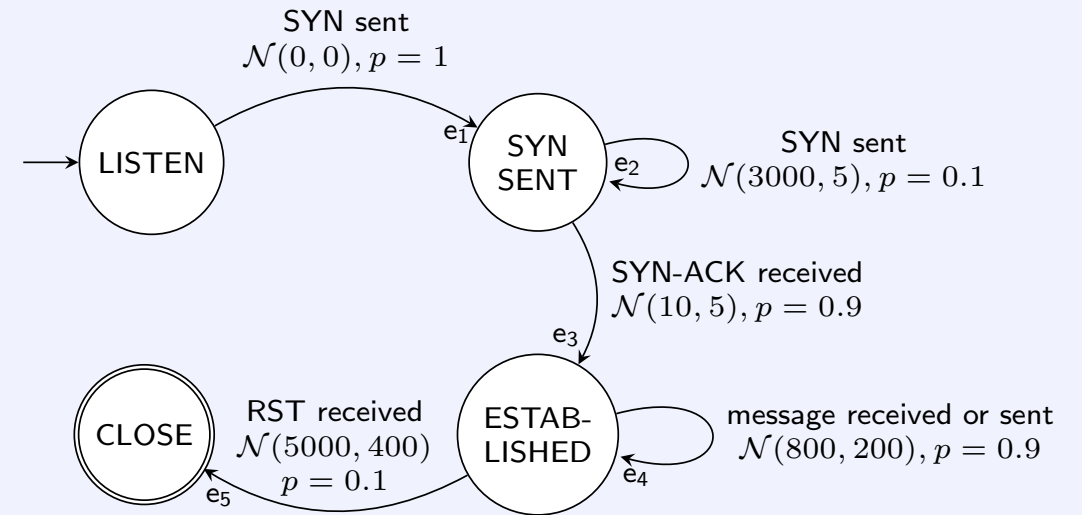
(SYN sent, 0),(ACK sent, 500),(SYN sent, 2000),(RST received, 6500)

correction

(SYN sent, 0),(SYN-ACK received, 10),(RST received, 6500)

(SYN sent, 0),(SYN sent, 2000),(SYN-ACK received, 10),(RST received, 6500)

...

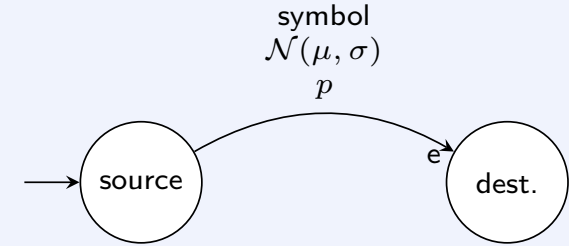


Many correction solutions possible...

We choose the one with the
minimal description length

Data encoding

Cost of a **followed** pair (symbol, delay)
corrected with (operation, transition, delay) depends on

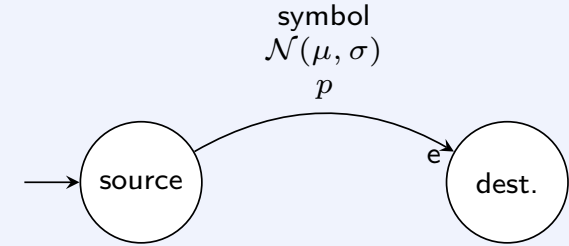


Data encoding

Cost of a **followed** pair (symbol, delay)
corrected with (operation, transition, delay) depends on

- The probability of the edit operation (follow),

$$-\log_2 p(o)$$

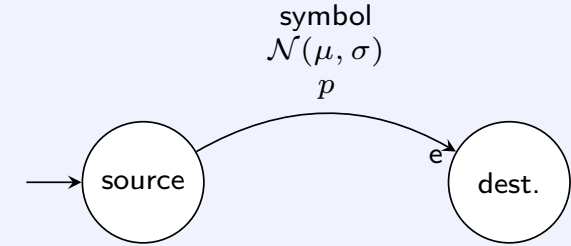


Data encoding

Cost of a **followed** pair (symbol, delay)

corrected with (operation, transition, delay) depends on

- The probability of the edit operation (follow),
- The probability of the transition given the current state,



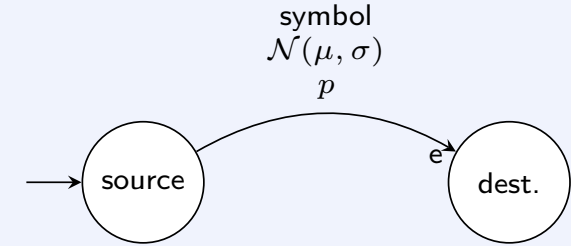
$$-\log_2 p(o) - \log_2 p(e|q_s(e))$$

Data encoding

Cost of a **followed** pair (symbol, delay)

corrected with (operation, transition, delay) depends on

- The probability of the edit operation (follow),
- The probability of the transition given the current state,
- The probability of the delay given the transition guard's parameters.



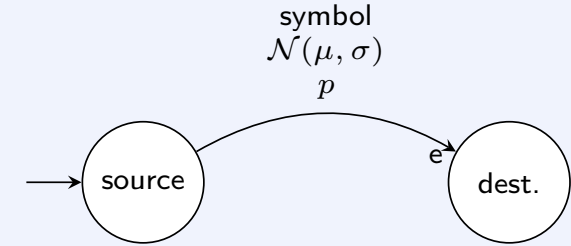
$$-\log_2 p(o) - \log_2 p(e|q_s(e)) - \log_2 p(d|e)$$

Data encoding

Cost of a **transposed** pair (symbol, delay)

corrected with (operation, transition, delay) depends on

- The probability of the edit operation (transpose),
- The probability of the transition given the current state,
- The probability of the delay given the transition guard's parameters.



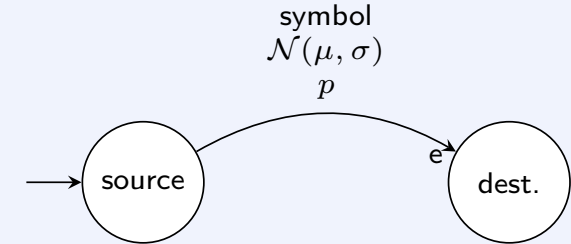
$$-\log_2 p(o) - \log_2 p(e|q_s(e)) - \log_2 p(d|e)$$

Data encoding

Cost of an **added** pair (symbol, delay)

corrected with (operation, transition, delay) depends on

- The probability of the edit operation (add),
- The probability of the transition given the current state,
- ~~The probability of the delay given the transition guard's parameters.~~



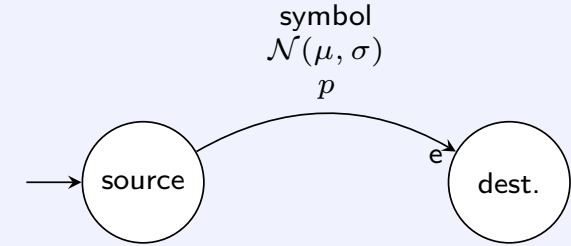
$$-\log_2 p(o) - \log_2 p(e|q_s(e))$$

Data encoding

Cost of a **deduplicated** pair (symbol, delay)

corrected with (operation, transition, delay) depends on

- The probability of the edit operation (deduplicate),
- ~~The probability of the transition given the current state,~~
- The probability of the delay given the transition guard's parameters.

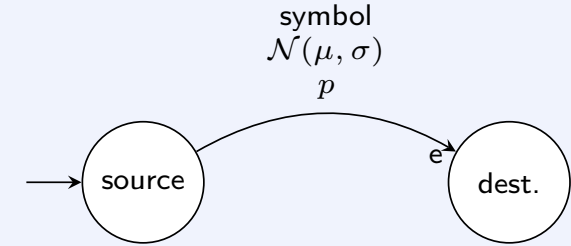


$$-\log_2 p(o) - \log_2 p(d|e)$$

Data encoding

Cost of a **skipped** pair (symbol, delay)
corrected with (operation, ε , delay) depends on

- The probability of the edit operation (skip),
- ~~The probability of the transition given the current state,~~
- ~~The probability of the delay given the transition guard's parameters.~~
- The cost of explicitly encoding the delay and the symbol.



$$-\log_2 p(o) + L_{\mathbb{N}}(d) + \log_2 |\Sigma|$$

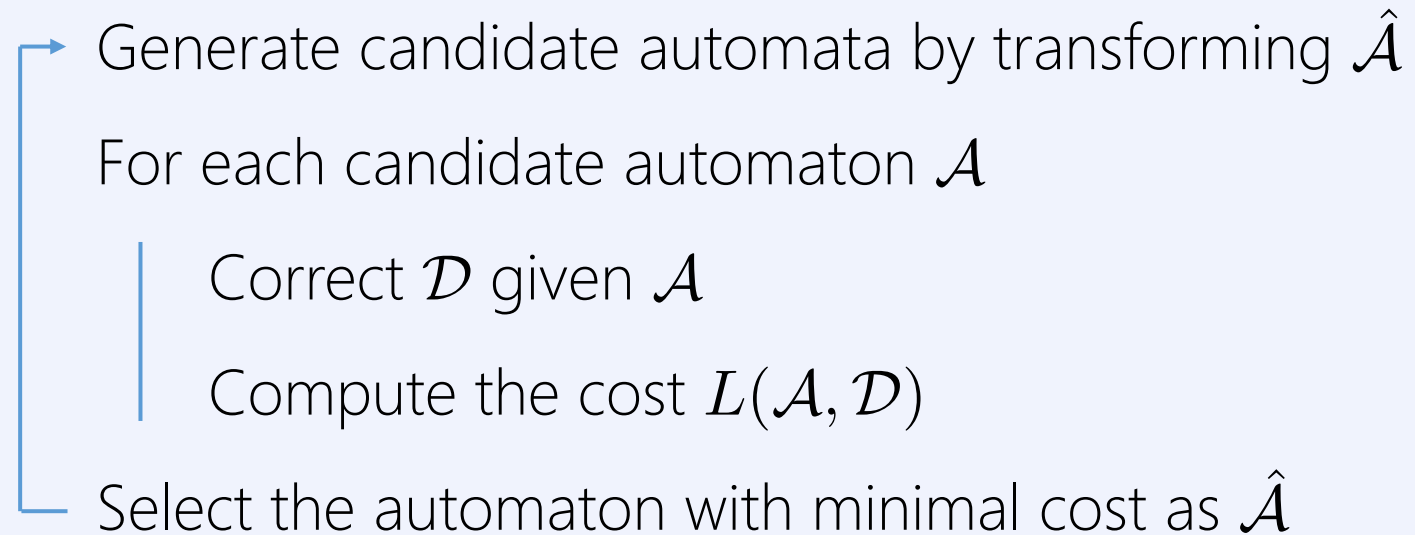
Question



How to **find** the automaton with the **minimal MDL cost**?

TADAM: MDL-based automata learning

Initialize an automaton $\hat{\mathcal{A}}$ with the data \mathcal{D}

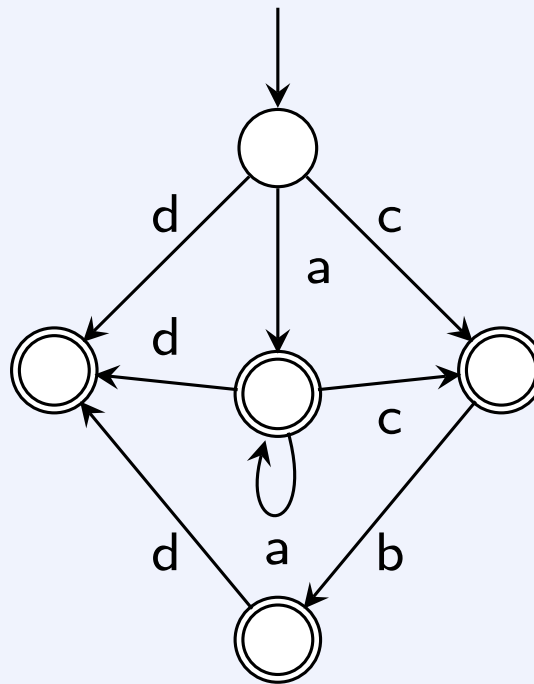


Return $\hat{\mathcal{A}}$ when the cost doesn't decrease anymore

Initialization

a c b
a d
c b a c
a c a
d a a
c b d

Markov initialization



guards and probabilities omitted

Candidate automata generation

Automaton transformation operations:

- Location merge
- Location split
- Subpart deletion

One candidate per possible transformation and position in the automaton

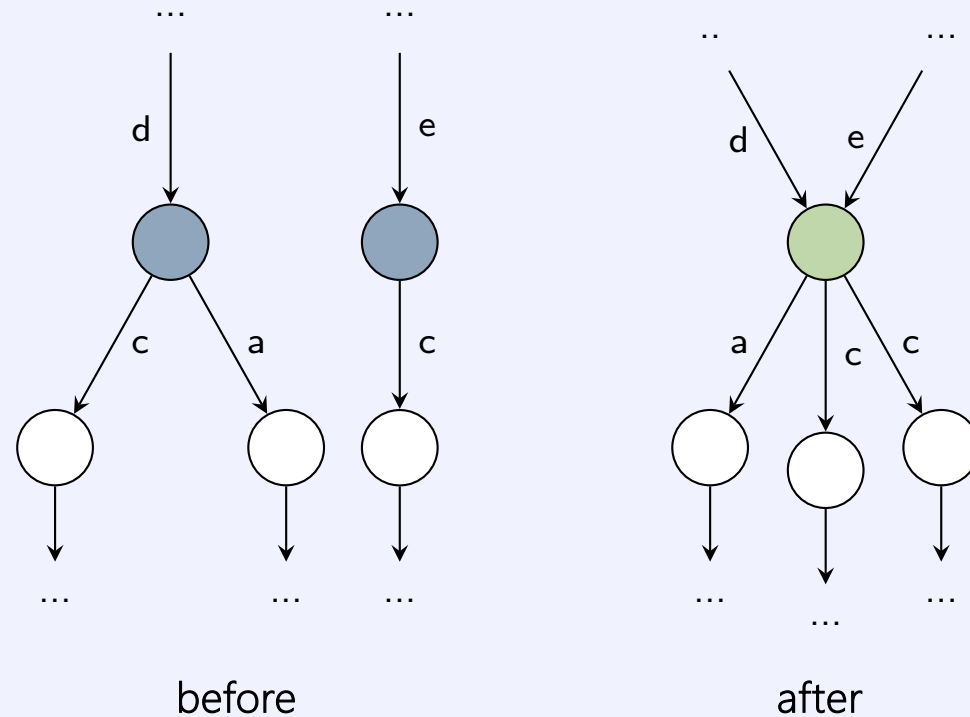
Location merge

Goal:

Reducing the size of the automaton and generalize the model
(reduces the model cost)

Side effect:

Increases the data cost



guards and probabilities omitted

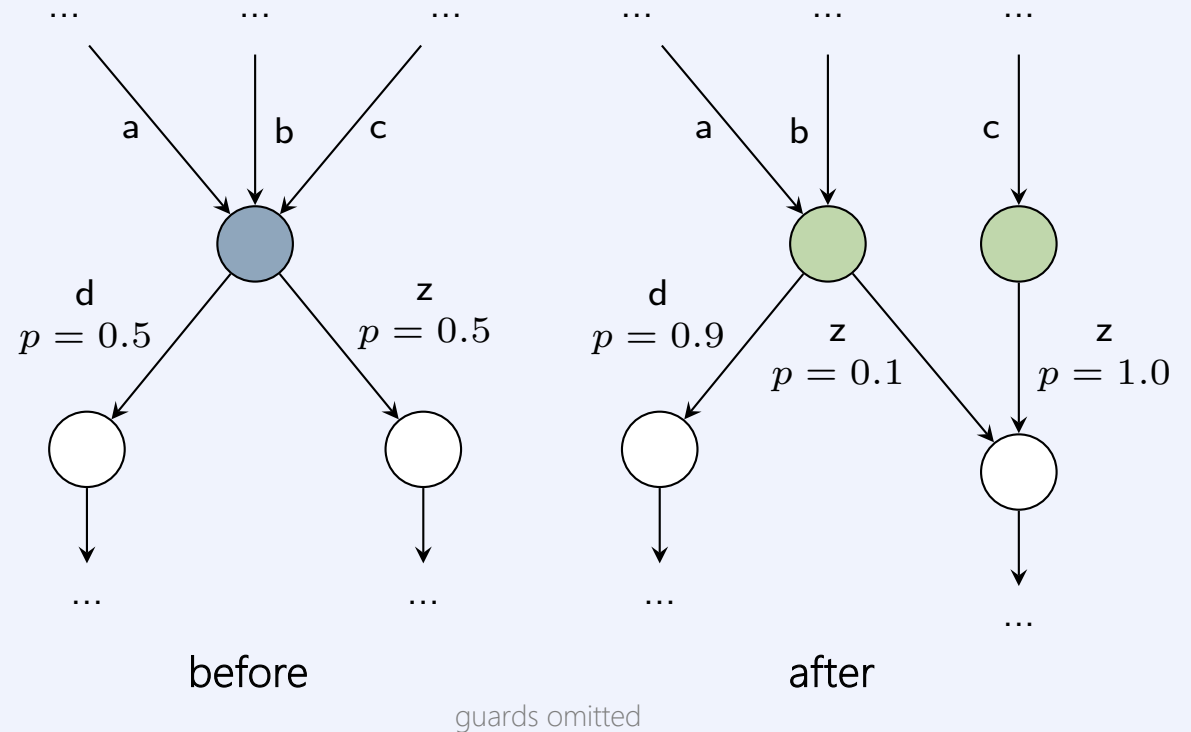
Location split

Goal:

Reducing the entropy of the
"next triggered transition" at
a given location
(reduces the data cost)

Side effect:

Increases the model cost



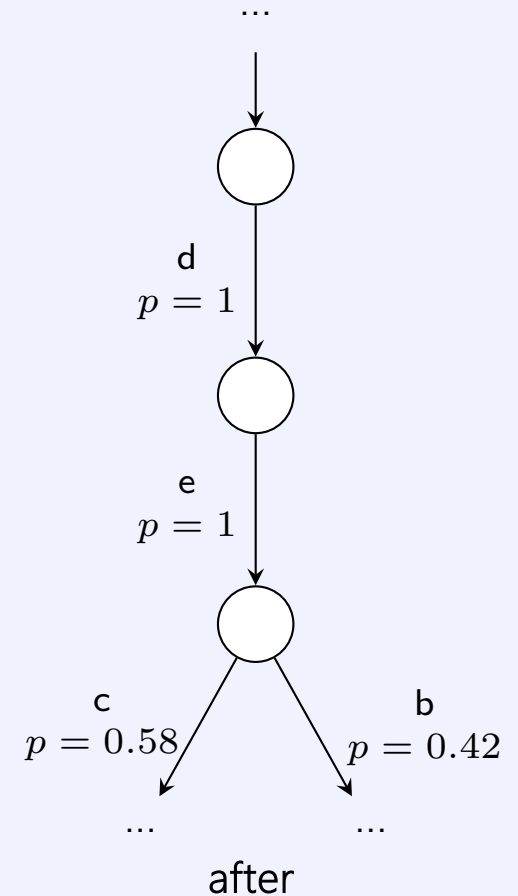
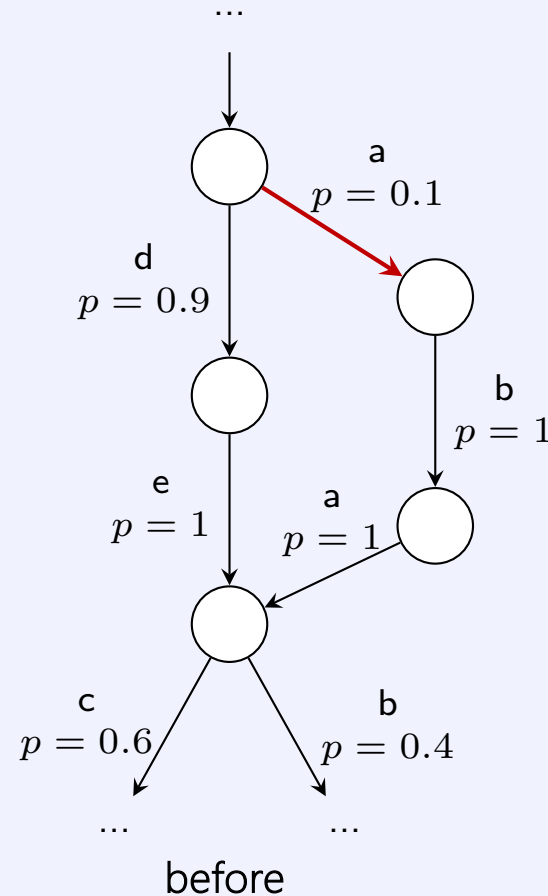
Subpart deletion

Goal:

Reducing the size of the automaton
(reduces the model cost)

Side effect:

Increases the data cost



guards omitted

Question



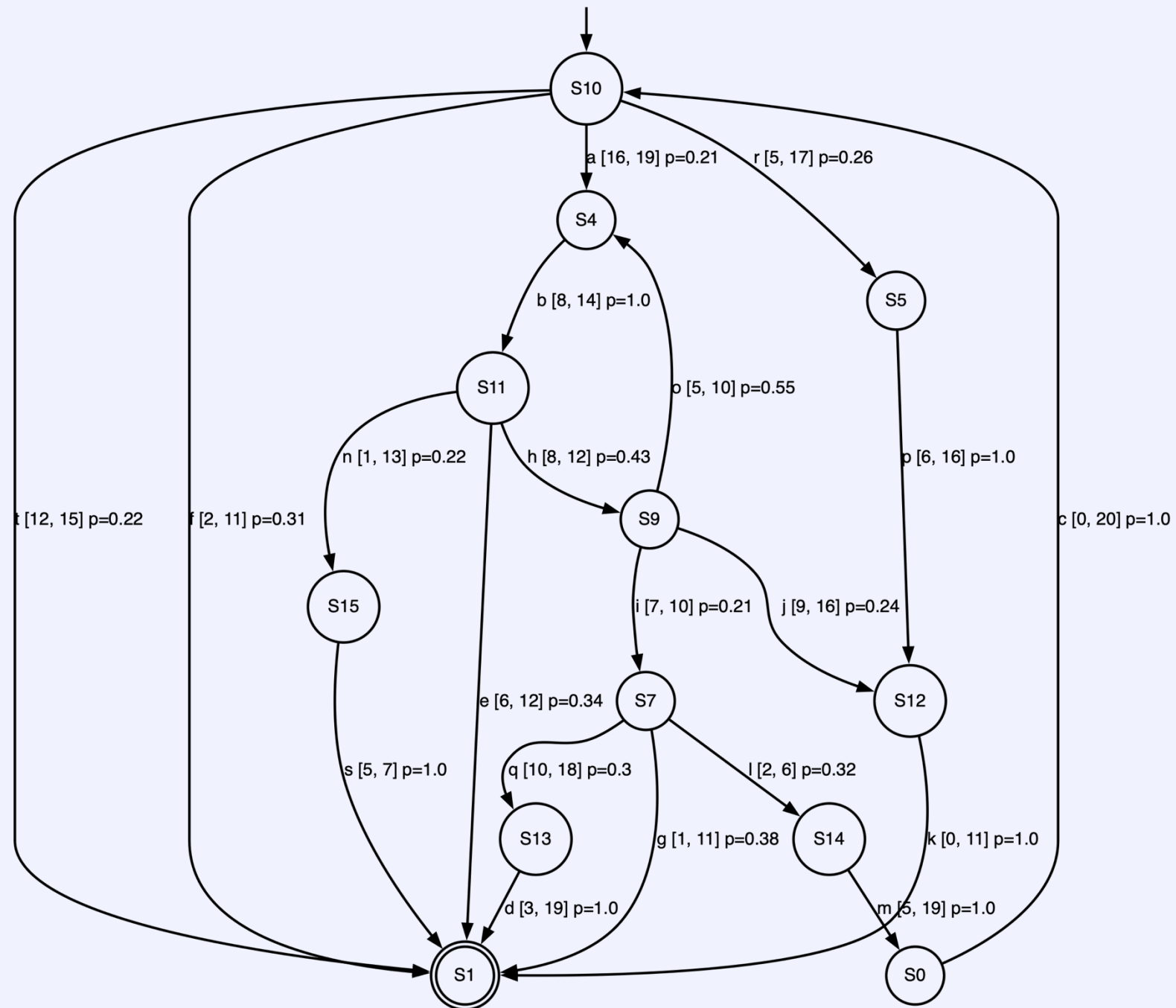
Does it **work**?

State of the Art

Algorithm	Strategy	Main limitation
TAG (Cornanguer et al., 2022)	Factorization on common sub-parts and location splits	
Timed k-Tail (Pastore et al., 2017)	Factorization on common sub-parts	No noise robustness strategy → requires clean data
RTI+ (Verwer et al., 2010)	Location merge based on likelihood test	

Experiments

Target automaton

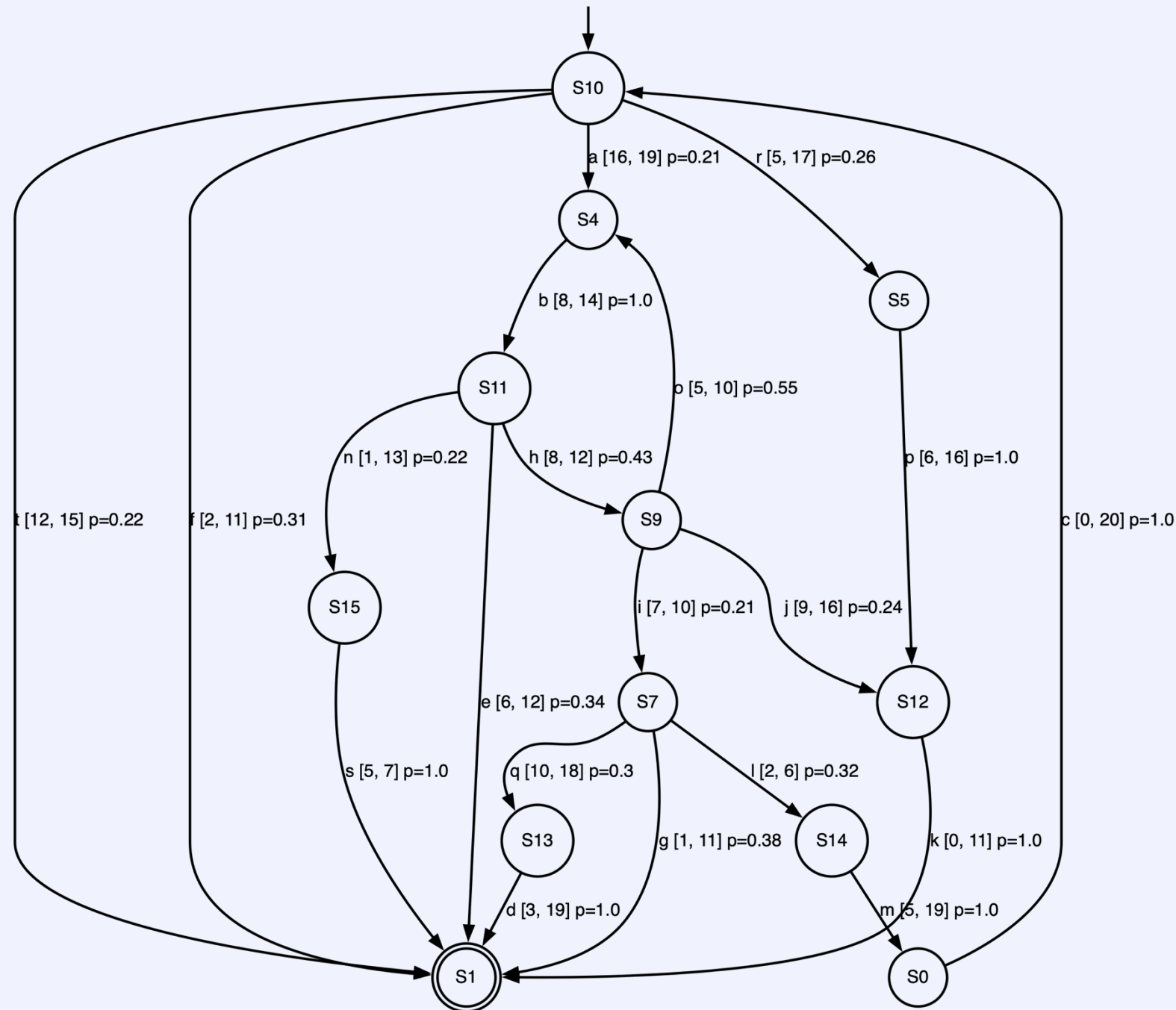


Experiments

Target automaton

Data:

- 500 timed words
- 2,5% of noisy events



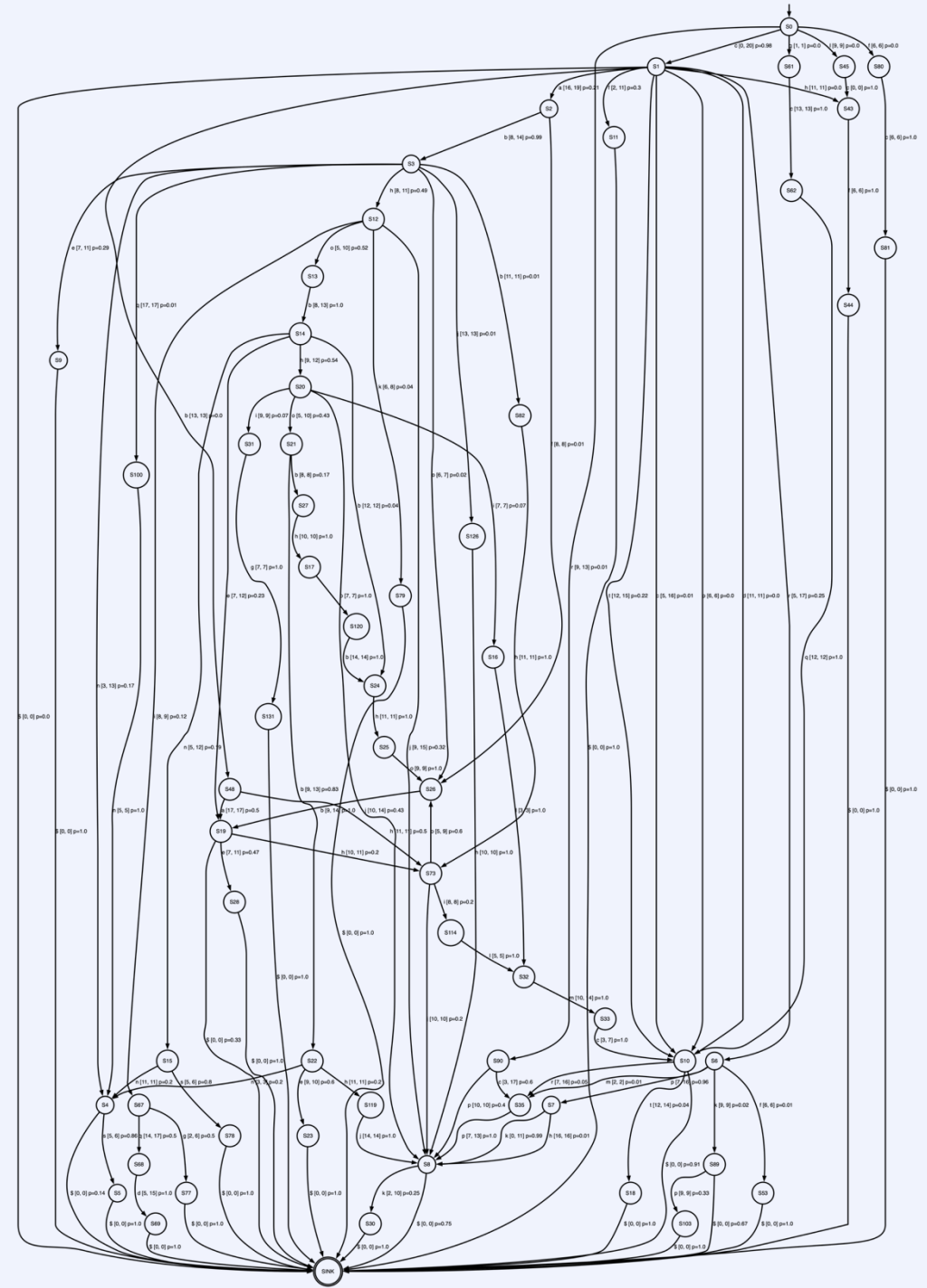
Experiments

TAG

learned automaton

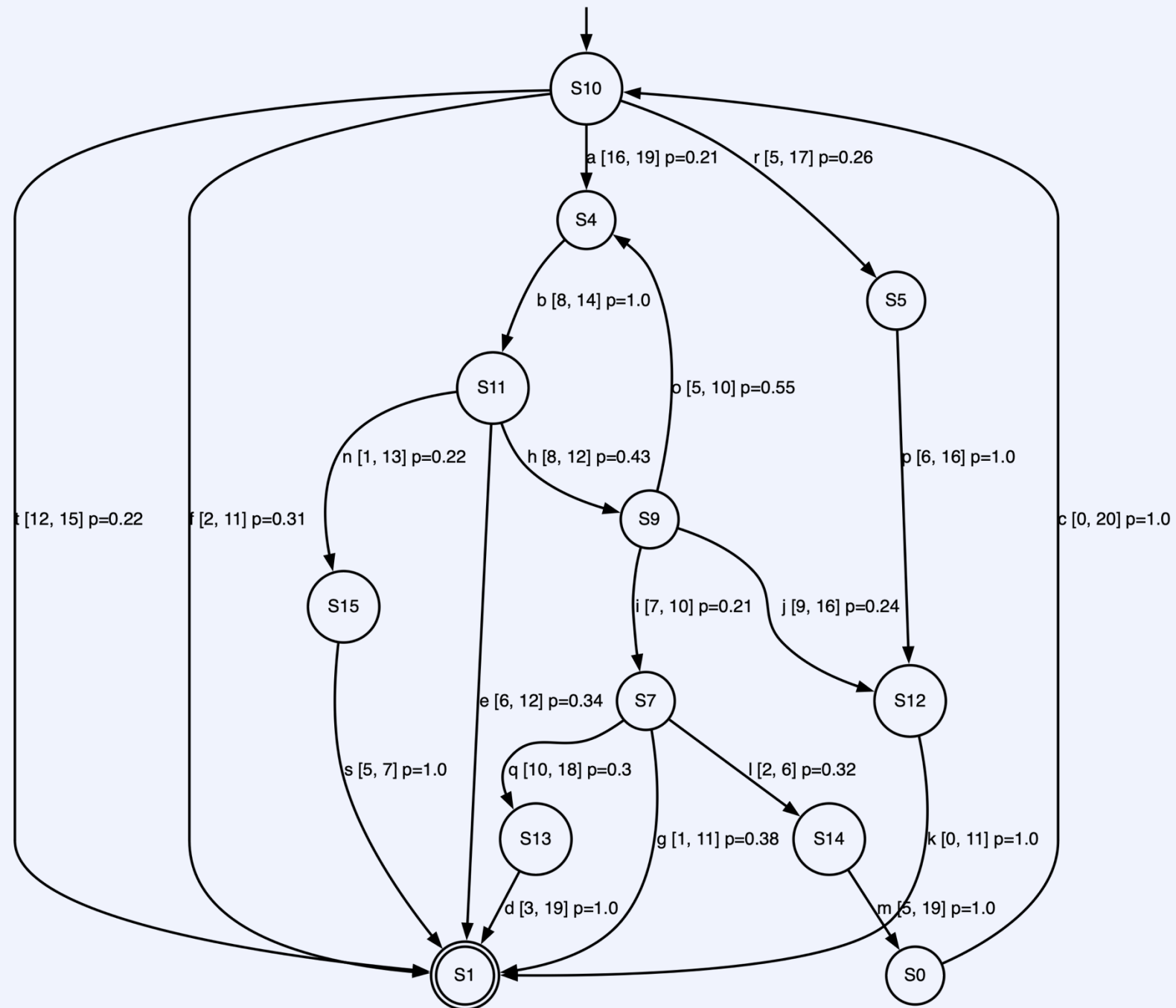
Data:

- 500 timed words
- 2,5% of noisy events



Experiments

Target automaton



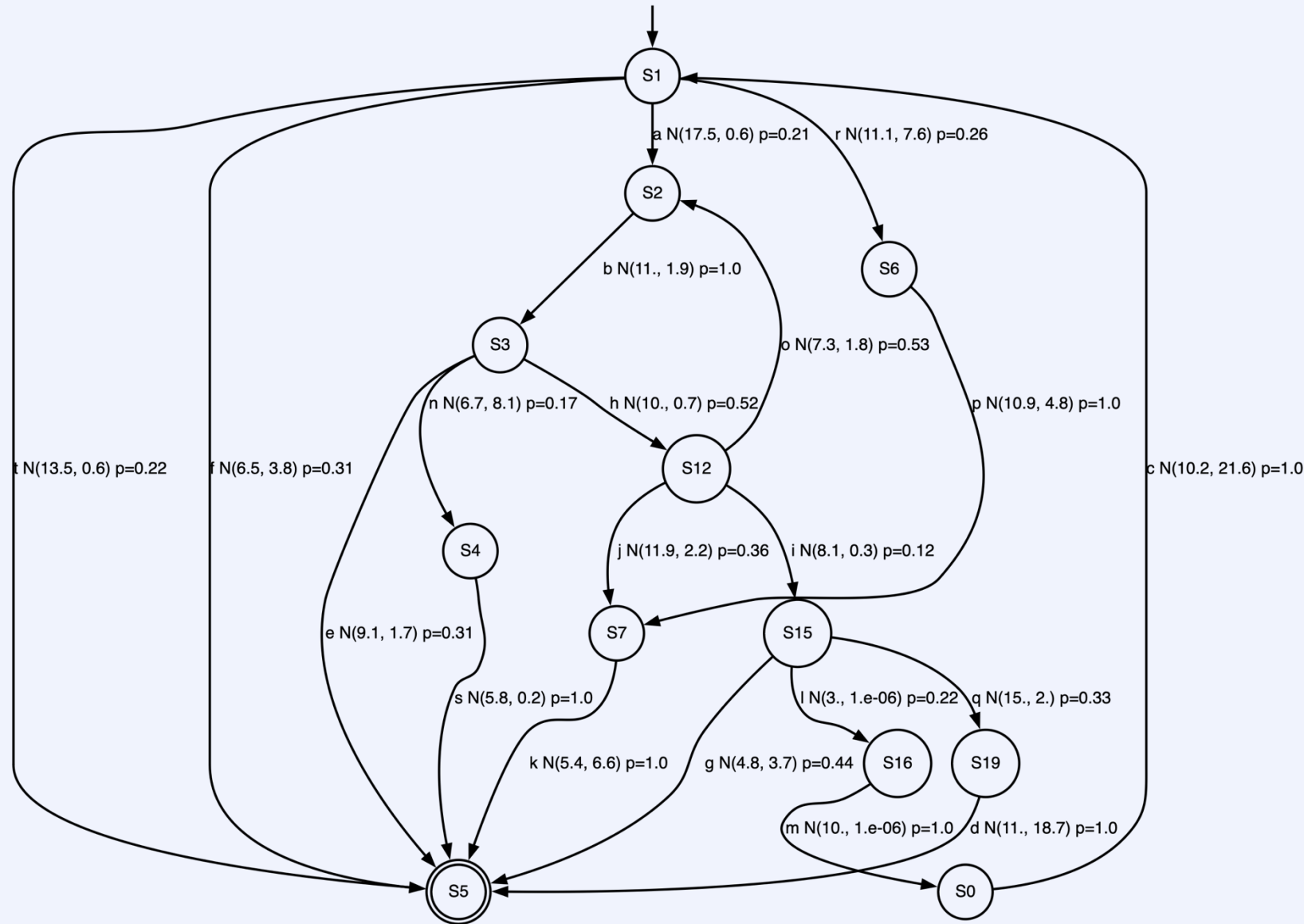
Experiments

TADAM

learned automaton

Data:

- 500 timed words
- 2,5% of noisy events



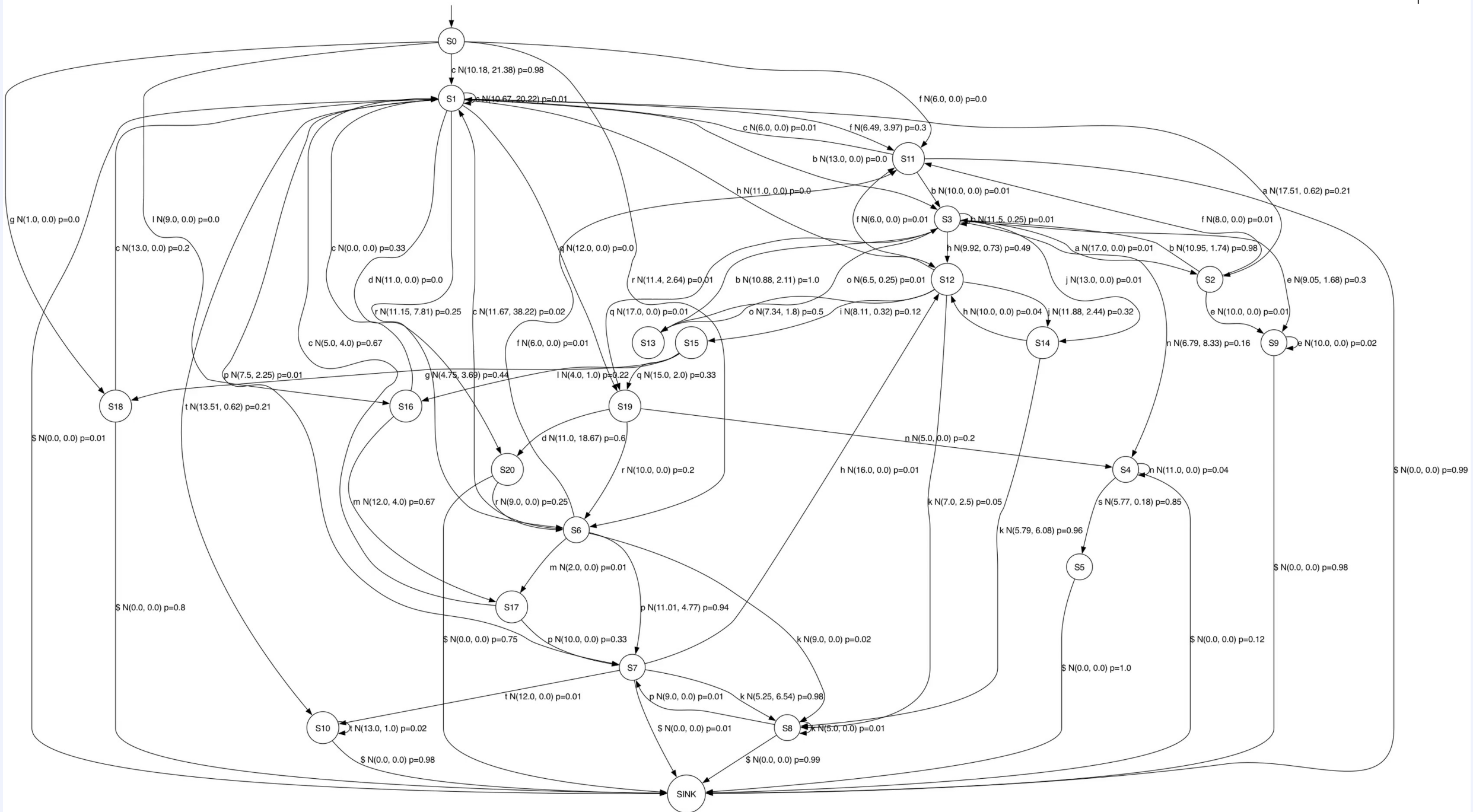
Experiments

TADAM

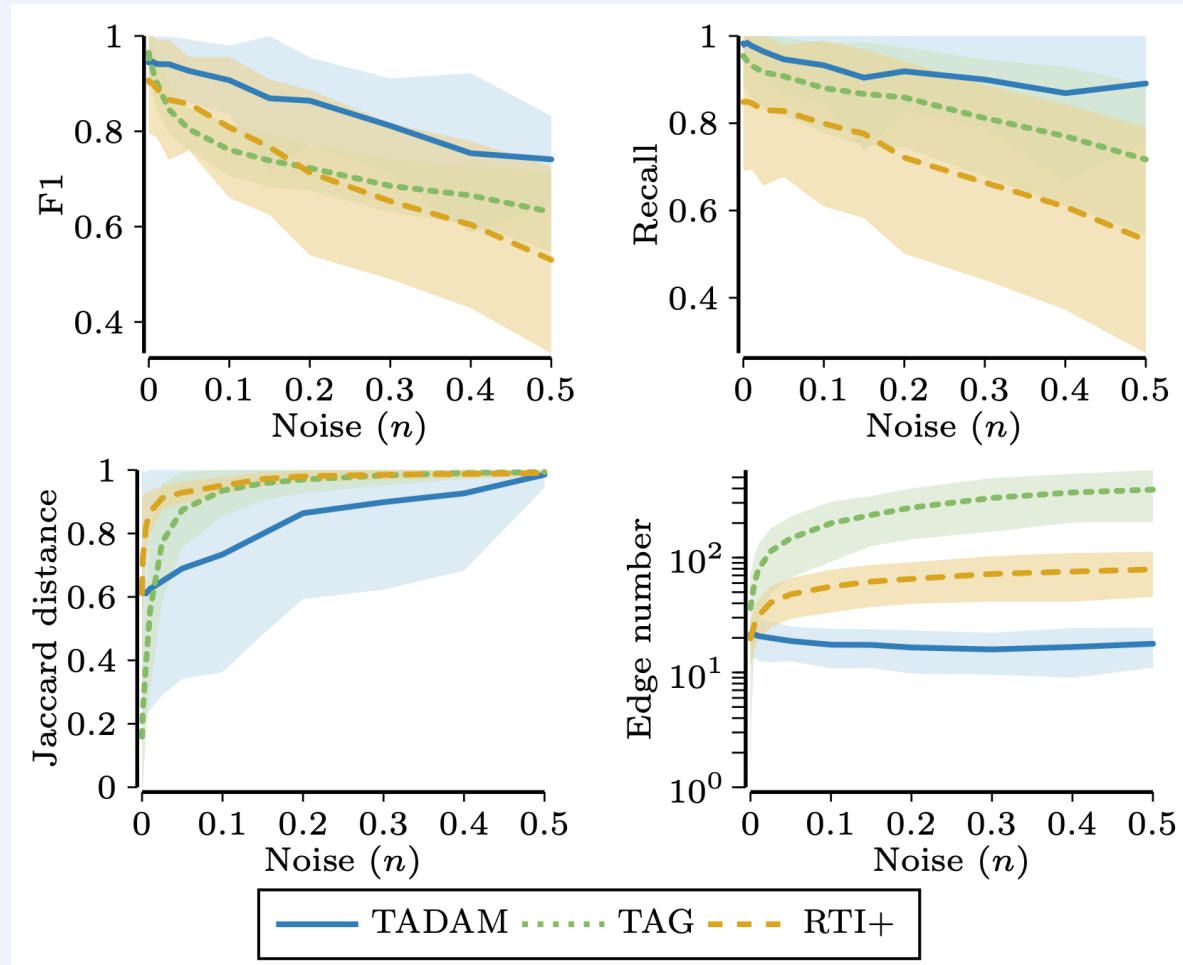
learned automaton

Data:

- 500 timed words
- 2,5% of noisy events



Experiments



Noise robustness
on synthetic data

Experiments

		Learner	AU-ROC	TPR	FPR	F1
TA learners	{	TADAM	0.982	0.998	0.025	0.705
		TAG	0.891	1	0.142	0.298
		RTI+	0.790	1	0.292	0.171
		Hidden Markov Model	0.608	0.640	0.085	0.288

Anomaly detection performances
on HDFS dataset¹

1. <https://github.com/ait-aecid/anomaly-detection-log-datasets>

Experiments

		Learner	AU-ROC	TPR	FPR	F1	
TA learners	{	TADAM	0.982	0.998	0.025	0.705	← very high detection rate and less false alarms
		TAG	0.891	1	0.142	0.298	
		RTI+	0.790	1	0.292	0.171	
		Hidden Markov Model	0.608	0.640	0.085	0.288	

Anomaly detection performances
on HDFS dataset¹

1. <https://github.com/ait-aecid/anomaly-detection-log-datasets>

Experiments

		Learner	AU-ROC	TPR	FPR	F1	
TA learners	{	TADAM	0.982	0.998	0.025	0.705	← very high detection rate and less false alarms
		TAG	0.891	1	0.142	0.298	↘ overfit on the training data and don't generalize well
		RTI+	0.790	1	0.292	0.171	
		Hidden Markov Model	0.608	0.640	0.085	0.288	

Anomaly detection performances
on HDFS dataset¹

1. <https://github.com/ait-aecid/anomaly-detection-log-datasets>

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Conclusions

Contributions:

- A compression-based (MDL) score to avoid overfitting
- An explicit modelization of the noise

Experiments show that TADAM

- is far more robust to noise
- learns smaller models
- has better performances on real-world classification and anomaly detection tasks

Thank you!


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 Fos-R/TADAM

```
pip install tadam-learner
```

See you at the poster session!

